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CCS Concepts: • Computing methodologies → Shape inference.

Additional Key Words and Phrases: 3D generation, structural reconstruction, level of detail, co-analysis, architectural models

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The supplementary materials provide additional technical details about Co-LOD, including D2 descriptor computation (Sec. [1\)](#page-0-0), Co-LOD for Single Building (Sec. [2\)](#page-0-1), and BSP implementation (Sec. [3\)](#page-1-0). Additionally, we outline the configurations of comparative methods and present more comprehensive results (Sec. [4\)](#page-1-1).

1 CALCULATION OF D2 DESCRIPTOR

Considering computation time, robustness, and fidelity, we opted for the D2 descriptor [\[Osada et al.](#page-1-2) [2002\]](#page-1-2) for shape measurement over more advanced deep shape descriptor solutions [\[Xie et al.](#page-1-3) [2017\]](#page-1-3). In order to compute the D2 descriptor for a given segment efficiently and reliably, we employ a specific pipeline outlined in Algorithm [1.](#page-0-2) Initially, we uniformly sample 10,000 points from the segment and apply anisotropic scaling to normalize them into a point cloud p_n [\[Kazhdan et al.](#page-1-4) [2004\]](#page-1-4), ensuring consistent shape representation. Subsequently, we randomly select 256×256 point pairs from p_n and calculate their distances, dividing them into 256 intervals for quantification. This process yields the initial 256 components of the D2 vector. Furthermore, we sample 10,000 normal vectors from the segment, randomly selecting 20,000 pairs and computing the angle between each pair. These angles are discretized into 10 bins within the [0, ¹⁸⁰] degree range, generating the remaining 10 components of the D2 vector.

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ALGORITHM 1: Calculation of D2 Descriptor

- 1: Input: Segment
- 2: Output: D2 Descriptor
- 3: // Sample points and apply transformations
- 4: sample_points \leftarrow uniform_sampling(seqment, 10000)
- 5: $normalized_cloud \leftarrow apply_transformations(sample_points)$
- 6: // Compute distance-based features
- 7: $dis_histogram \leftarrow compute_dis_histogram(normalized_cloud)$
- 8: // Compute angle-based features
- 9: angle histogram \leftarrow compute angle histogram(segment)
- 10: // Combine distance and angle histograms to form D2 vector
- 11: return concatenate(distance_histogram, angle_histogram)

2 CO-LOD FOR SINGLE BUILDING

To conduct database-based single building analysis, we need to establish a component database and convert the LOD hierarchical method designed for co-analysis into a form that allows analyzing individual buildings. We'll explain these two steps and present the results of our single-building analysis.

Database Construction. We manually selected 90 representative structural segments from Composite Scene that represent building components outside the primary architectural structure. These segments enable us to hierarchically classify the components within individual buildings.

Method. Compared to the original Co-LOD algorithm, we adapt the LOD hierarchy derived from co-analysis to a format suitable for data-driven examination while maintaining other algorithmic components. For a building model divided into structural segments, we calculate $f_r(s)$ and $f_s(s)$ using the same approach as in co-analysis:

$$
f_r(s) = \text{IoU}(s, I) = \text{IoU}(P(s), P(I)),\tag{1}
$$

$$
f_s(s) = -\frac{\text{area}(s)}{\text{area}(I)},
$$
\n⁽²⁾

where $P(X)$ represents the discrete sampled point set of structural
segments X and I represents all segments of the model. To incorpor segments X, and I represents all segments of the model. To incorporate the structural segments from the database into our analysis, we introduce a new term, $f'_{co}(s)$, replacing the original f_{co} . This new term is defined as: term is defined as:

$$
f'_{co}(s) = \sum_{s' \in S_d} e^{-dis(s, s')},
$$
\n(3)

where s is a segment, and S_d represents the collection of structural
segments in the database. These three terms substitute the ontisegments in the database. These three terms substitute the optimization equation in co-analysis to determine whether a segment

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Fig. 1. Relationship between the runtime of the Polygonal Mesh Extraction stage and the number of detected planes. Compared to KSR, our method efficiently handles a greater number of input planes.

belongs to LOD0. Segments exhibiting a positive weighted sum are classified as LOD0, where the weights assigned to each item are consistent with those defined during co-analysis. Remaining segments are then clustered and assigned to higher LOD levels.

This method effectively achieves database-based LOD generation for individual buildings, as tested on Campus and European City, with statistical results shown in Table [1](#page-1-5) and visual results in Fig. [2.](#page-2-0) Co-LOD for single building proved more effective in datasets similar to the database (Campus). However, the performance on datasets beyond the database scope (European City) was significantly inferior to that based on co-analysis. This is reflected in the higher complexity of the generated LOD0 models and the lack of corresponding improvements in reconstruction accuracy.

3 POLYGONAL MESH EXTRACTION - BSP

We provide the pseudocode for the spatial partitioning strategy outlined in the Polygonal Mesh Extraction section (refer to Algorithm [2\)](#page-1-6). Our Polygonal Mesh Extraction approach is more efficient than KSR, as demonstrated by the runtime comparison in Fig. [1,](#page-1-7) where the KSR implementation is sourced from CGAL 6.0.

4 COMPARATIVE EXPERIMENT SETTINGS AND ADDITIONAL RESULTS

The experimental setup for the comparison methods PolyFit, KSR, LowPoly, QEM, and RobustLowPoly is outlined as follows. For Poly-Fit, the plane detection parameters were configured with a maximum distance (d_{max}) of 0.5, a minimum region size (s_{min}) of 1000, and a maximum angle (θ_{max}) of 30 degrees. For KSR, we empirically established three parameter configurations to generate models with varying levels of detail, defined by tuples: d_{max} at 0.5, 0.3, and 0.1, s_{min} at 2000, 500, and 100, and θ_{max} consistently set at 30 degrees across all settings. For LowPoly, we used the results produced by the official executable. Since other methods automatically generate their results, we utilized the automatically generated Carved Mesh as the final result without manually selecting from the provided pareto curve. Additionally, if results are not produced within an hour, we replace the original input with our highest LOD model with fewer

ALGORITHM 2: Binary Space Partition
Input: A set of planes, denoted as P
Output: Partitioned space defined by subspaces
Compute the bounding box (bbox) containing all planes in P 1
Create an empty queue of spaces to be partitioned, q_s 2
// Enqueue the initial bounding box to the partition queue 3
q_s .push(bbox) $\overline{\bf 4}$
while q_s is not empty do 5
// Dequeue the next space to be partitioned 6
Remove and retrieve the next space S_p from q_s 7
Extract the largest plane p from S_p for partitioning 8
Divide S_p into two subspaces S_p^1 and S_p^2 using p 9
// Distribute remaining planes to their respective subspaces 10
for each plane p' in S_p do 11
if p' belongs to S_p^1 then 12
Assign p' to S_p^1 13
end 14
if p' belongs to S_p^2 then 15
Assign p' to S_p^2 16
end 17
end 18
// Enqueue non-empty subspaces back to the partition queue 19
if S_p^1 contains planes then 20
q_s .push (S_p^1) 21
end 22
if S_p^2 contains planes then 23
q_s .push (S_p^2) 24
end 25
end 26

Table 1. Statistics of Co-LOD in different LOD0 generation tasks. S: single building analysis, Co: co-analysis based on the scene.

facets to ensure effective output within a reasonable time frame. For both QEM and RobustLowPoly, we reduce the model faces to match the corresponding LOD for fair comparisons.

In Fig. [3,](#page-3-0) we further demonstrate the results obtained on Composite Scene. Figs. [4-](#page-4-0)[33](#page-33-0) show the randomly selected individual models used in the user study, and Figs. [34-](#page-34-0)[39](#page-39-1) display the scenes employed in the user study. For individual models, we restricted our selection to models with over 1,000 facets to ensure diversity.

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Fig. 2. Comparison of Co-analysis and Co-LOD for Single Building Analysis on Campus (top) and European City (bottom).

1:4 • R. Zhang, S. Pan, C. Lv, M. Gong, and H, Huang

Fig. 3. Further LOD generation results by Co-LOD for Composite Scene.

Fig. 4. Qualitative comparisons of randomly selected cases (1/30).

Fig. 5. Qualitative comparisons of randomly selected cases (2/30).

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Fig. 6. Qualitative comparisons of randomly selected cases (3/30).

Fig. 7. Qualitative comparisons of randomly selected cases (4/30).

Fig. 8. Qualitative comparisons of randomly selected cases (5/30).

Fig. 9. Qualitative comparisons of randomly selected cases (6/30).

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Fig. 10. Qualitative comparisons of randomly selected cases (7/30).

Fig. 11. Qualitative comparisons of randomly selected cases (8/30).

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Fig. 12. Qualitative comparisons of randomly selected cases (9/30).

Fig. 13. Qualitative comparisons of randomly selected cases (10/30).

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Fig. 14. Qualitative comparisons of randomly selected cases (11/30).

Fig. 15. Qualitative comparisons of randomly selected cases (12/30).

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Fig. 16. Qualitative comparisons of randomly selected cases (13/30).

Fig. 17. Qualitative comparisons of randomly selected cases (14/30).

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Fig. 18. Qualitative comparisons of randomly selected cases (15/30).

Fig. 19. Qualitative comparisons of randomly selected cases (16/30).

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Fig. 20. Qualitative comparisons of randomly selected cases (17/30).

Fig. 21. Qualitative comparisons of randomly selected cases (18/30).

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Fig. 22. Qualitative comparisons of randomly selected cases (19/30).

Fig. 23. Qualitative comparisons of randomly selected cases (20/30).

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Fig. 24. Qualitative comparisons of randomly selected cases (21/30).

Fig. 25. Qualitative comparisons of randomly selected cases (22/30).

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Fig. 26. Qualitative comparisons of randomly selected cases (23/30).

Fig. 27. Qualitative comparisons of randomly selected cases (24/30).

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Fig. 28. Qualitative comparisons of randomly selected cases (25/30).

Fig. 29. Qualitative comparisons of randomly selected cases (26/30).

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Fig. 30. Qualitative comparisons of randomly selected cases (27/30).

Fig. 31. Qualitative comparisons of randomly selected cases (28/30).

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Fig. 32. Qualitative comparisons of randomly selected cases (29/30).

Fig. 33. Qualitative comparisons of randomly selected cases (30/30).

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Architectural Co-LOD Generation (Supplementary Materials) • 1:35

Fig. 34. Qualitative comparisons of Research Center.

Fig. 35. Qualitative comparisons of Town.

Fig. 36. Qualitative comparisons of Metropolis.

Fig. 37. Qualitative comparisons of Campus.

ACM Trans. Graph., Vol. 43, No. 6, Article 1. Publication date: December 2024.

Fig. 38. Qualitative comparisons of European City.

Fig. 39. Qualitative comparisons of Suburbia.